

State Space Problem Solving Model for the Missionaries and Cannibals Problem

1. PROBLEM STATEMENT

There are three Missionaries (M) and three Cannibals (C), and one boat on a river that fits at most two people. At least one person is required to operate the boat. All six missionaries and cannibals must safely cross the river – under one condition; at no point should the number of cannibals outnumber the missionaries at any spot (left bank, right bank, boat) – otherwise, the missionaries will be consumed.

2. THE OBJECTS OF THE WORLD

- Three Missionaries
- Three Cannibals
- Three spots: The boat, the left bank and the right bank

3. REPRESENTATION OF A STATE IN THE WORLD

- Let m be the number of marines in a given spot
- Let c be the number of cannibals in a given spot
- Let B , LB and RB represent the Boat, Left Bank and Right Bank respectfully
- A state will be represented as: $\{ LB = (m,c) \mid B = (m,c) \mid RB = (m,c) \mid m = 0,1,2,3 \mid c = 0,1,2,3 \mid m \geq c \mid m+c < 2 \text{ for } B \}$

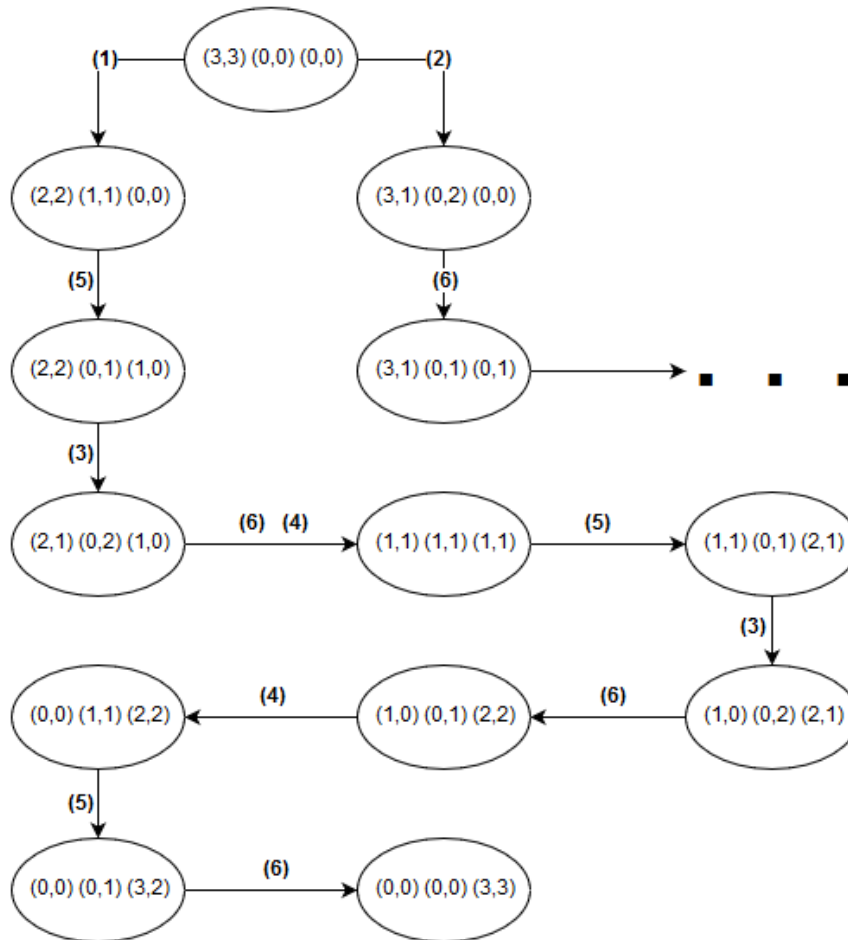
4. THE STATE SPACE DESCRIPTION

- Initial State: $\{ LB = (3,3) \mid B = (0,0) \mid RB = (0,0) \}$
- Goal State: $\{ LB = (0,0) \mid B = (0,0) \mid RB = (3,3) \}$

5. PARTIAL STATE SPACE GRAPH/TREE

- State Space Operators:
 - (1) Place 1 M and 1 C on boat: $LB = (m-1,c-1) \mid B = (1,1) \mid RB = (m,c)$
 - (2) Place 2 C's on boat: $LB = (m,c-2) \mid B = (0,2) \mid RB = (m,c)$
 - (3) Place 1 C on boat (C already controlling boat): $LB = (m,c-1) \mid B = (0,2) \mid RB = (m,c)$
 - (4) Place 1 M on boat (C already controlling boat): $LB = (m-1,c) \mid B = (1,1) \mid RB = (m,c)$
 - (5) Drop M on RB: $LB = (m,c) \mid B = (0,1) \mid RB = (m+1,c)$
 - (6) Drop C on RB: $LB = (m,c) \mid B = (0,1) \mid RB = (m,c+1)$

Graph is on next page



6. STATE SPACE SOLUTION

<u>Step</u>	<u>State</u>
-	(3,3) (0,0) (0,0)
(1)	(2,2) (1,1) (0,0)
(5)	(2,2) (0,1) (1,0)
(3)	(2,1) (0,2) (1,0)
(6)	(2,1) (0,1) (1,1)
(4)	(1,1) (1,1) (1,1)
(5)	(1,1) (0,1) (2,1)
(3)	(1,0) (0,2) (2,1)
(6)	(1,0) (0,1) (2,2)
(4)	(0,0) (1,1) (2,2)
(5)	(0,0) (0,1) (3,2)
(6)	(0,0) (0,0) (3,3)